



**TÉCNICO**  
LISBOA



# *Waste Collection with Route Balancing Concerns: A real-world application*

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# Context



- Waste collection of recyclable materials has been shown to possess great potential for improvement.

Gonçalo et. al. 2014 discovered that only 40% of the recyclable waste bins collected by a waste collection company (Valorsul) presented a fill level higher than 75%.

↳ Need to improve efficiency of collection routes

Table I - Characterization of improved routes at ValorSul, on average.

	Duration (min.)	Distance (km)	# Containers
Max.	478,8	255	101
Min.	379,1	100	32
Range	99,7	155	69

↳ Highly imbalanced routes

- The improvement of the efficiency in waste collection routes frequently leads to imbalanced solutions regarding duration, distance.

↳ How to consider balancing concerns when routing for waste collection?



# Case-Study

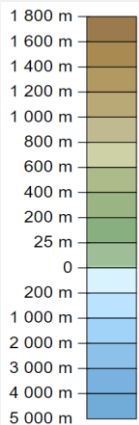


## ■ New Partner: ERSUC

### Concerns:

- Imbalance between collection routes generates dissatisfaction amongst drivers.
  - The characteristics of the **terrain** should also be considered.

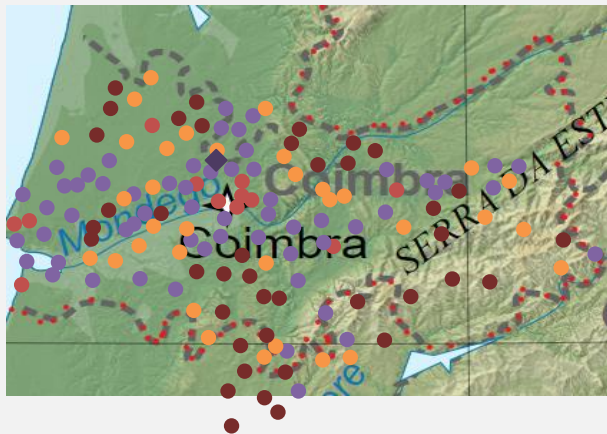
### Altitude



# Objective



To determine static recyclable waste collection routes, considering balancing concerns.



- Cluster 0
- Cluster 1
- Cluster 2
- Cluster 3
- ◆ Depot

## Case-Study characteristics

- **Network:** Symmetric;
- **Demand:** Containers are aggregated per town. The demand for each town is static for fixed periods of time;
  - Cluster towns by time interval between collections.
  - Material considered is Plastic/Metal;
- **Fleet:** Homogeneous of capacity | 620 kg;
  - Capacity = 90% of full capacity, | 800 kg.
- **Costs:** | €/km;
- **Objectives:** Minimize total distance while considering balancing concerns.

	Time interval	# Towns
Cluster 0	< 7days	15
Cluster 1	[7-14[	59
<b>Cluster 2</b>	<b>[14-21[</b>	<b>34</b>
Cluster 3	>21	42

## 1) Literature Review

- What metrics can we use to measure workload balance?

## 2) Extend a CVRP formulation to incorporate balancing metrics.

- What impacts can we expect when we choose one metric over another?

# Literature Review



## Literature Review methodology

### Search stage:

- Search in Web of Knowledge the key-words: Vehicle Routing Problems Route Balancing (34 articles, many irrelevant and one interesting review)
- Selection of the most relevant articles and look-up articles cited by the review and citing it.

## Relevant Review articles:

- [1] Jozefowicz, N., Semet, F., & Talbi, E.-G. (2008). *Multi-objective vehicle routing problems*. European Journal of Operational Research, 189(2), 293–309. <https://doi.org/10.1016/J.EJOR.2007.05.055>
- [2] Matl, P., Hartl, R. F., & Vidal, T. (2016). *Workload Equity in Vehicle Routing Problems: A Survey and Analysis*. (September), 0–22. <https://doi.org/10.1287/trsc.2017.0744>
- [3] Kovacs AA, Golden BL, Hartl RF, P. S. (2014). *Vehicle Routing Problems in Which Consistency Considerations are Important: A Survey*. *Networks*, 64(3), 192–213. <https://doi.org/https://doi.org/10.1002/net.21565>

## Most common routing objectives in VRP:

- **Cost;**
- **Makespan;**
- **Balance;**
- **Profit;**
- **Risk;**
- **Regionalization/Districting**



Fairness/Equity of workload distribution:

- Makespan,
- Balance,
- Regionalization/Districting

## Fairness/Equity of workload distribution:

### Objectives

- **Makespan: Minimization of the maximum route length.**
  - Metric: distance/duration [4,6].
  
- **Regionalization/Districting: Creation of geographical clusters used as input for routing. [11]**
  - Applicability associated with demand uncertainty [3].
  
- **Balance: widely varied [2]**
  - Metric: Length (**distance, duration**), **Demand** (weight, #customers)
  - Function: Range, Min-Max, Standard Deviation, Absolute Deviation to the mean.



# Literature Review



## Modeling Approaches

### Single-Objective

- Primary objective, PO
- Constraint, C

### Multi-Objective

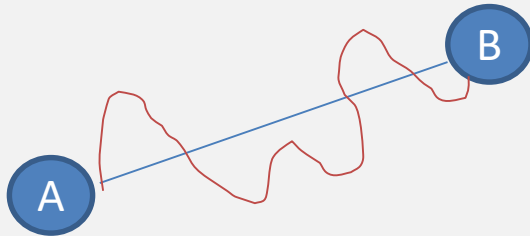
- Weighted Sum, WS
- Multiobjective methods, MOm ( $\epsilon$ -constraint method)

In Matl, P. et. al. 2016 it is possible to conclude that, when modeling balancing concerns:

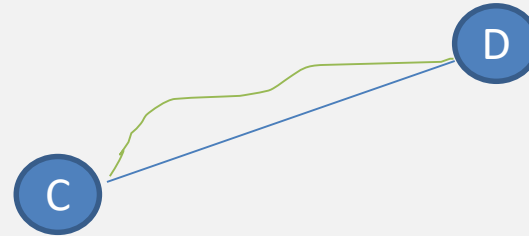
- Many more works with heuristics (50 heuristic methods to 11 exact )
- The most frequent functions are: min-max and range.



# New Metric - Ruggedness



Highly rugged area



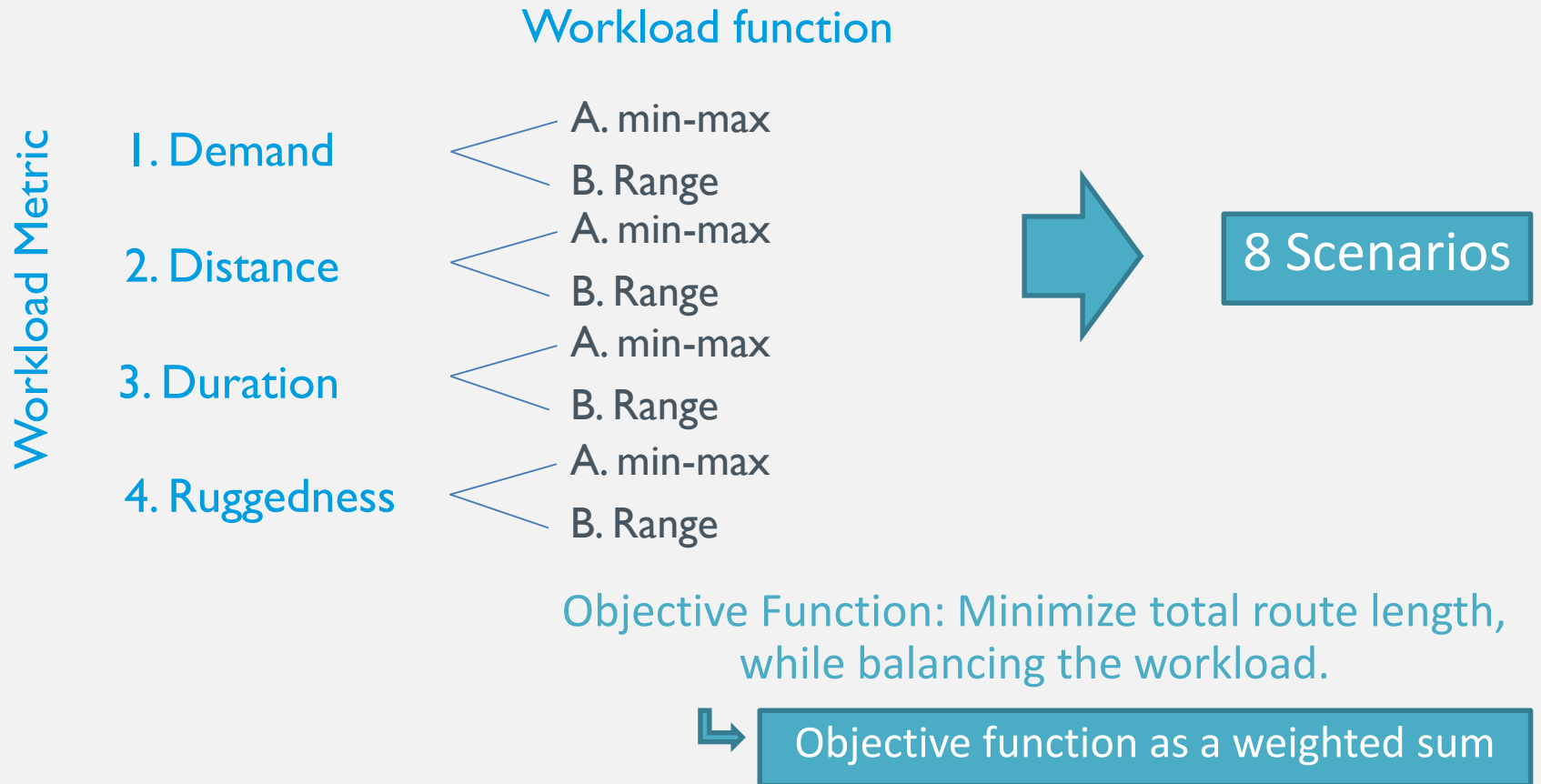
Normal area

**Ruggedness Coefficient calculation:**

$$coef_{ij} = \frac{RealDistance_{ij}}{EuclidianDistance_{ij}} \times 100$$

- Associates, on average, higher coefficients to regions the company believes to have more ruggedness.

# Scenarios



## 1. Demand : Number of containers to collect

$$\text{Workload}_k = \sum_i b_{ik} \times \text{NbContainers}_i$$

## 2.Distance : Distance inter-towns and intra-towns

$$\text{Workload}_k = \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times \text{NbContainers}_i \times DBC$$

## 3. Duration : Time to travel inter and intra-towns + plus container collection time

$$\text{Workload}_k = \sum_{ij} x_{ijk} \times d_{ij} \times \text{InvInter} + \sum_i b_{ik} \times \text{NbContainers}_i \times DBC \times \text{InvIntra} + \sum_i b_{ik} \times \text{NbContainers}_i \times ACT$$

## 4. Ruggedness : To associate each arc with a “terrain difficulty” measure

$$\text{Workload}_k = \sum_{ij} x_{ijk} \times \text{coef}_{ij}$$

# Scenarios (I)



## 1. Demand

$$\text{A. Max } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_i b_{ik} \times NbContainers_i \right)$$

$$\text{B. Range } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_i b_{ik} \times NbContainers_i \right) - \min_k \left( \sum_i b_{ik} \times NbContainers_i \right)$$



Total Distance

## 2. Distance

$$\text{A. Max } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right)$$

$$\text{B. Range } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right) - \min_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right)$$

# Scenarios (II)



## 3. Duration

$$\text{A. Max } \sum_{ijk} x_{ijk} \times d_{ij} \times IInterv \\ + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} \times IInterv + \sum_i b_{ik} \times NbContainers_i \times DBC \times IIntrav + \sum_i b_{ik} \times NbContainers_i \times ACT \right)$$

$$\text{B. Range } \sum_{ijk} x_{ijk} \times d_{ij} \times IInterv \\ + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} \times IInterv + \sum_i b_{ik} \times NbContainers_i \times DBC \times IIntrav + \sum_i b_{ik} \times NbContainers_i \times ACT \right) \\ - \min_k \left( \sum_{ij} x_{ijk} \times d_{ij} \times IInterv + \sum_i b_{ik} \times NbContainers_i \times DBC \times IIntrav + \sum_i b_{ik} \times NbContainers_i \times ACT \right)$$

## 4. Ruggedness Coefficient

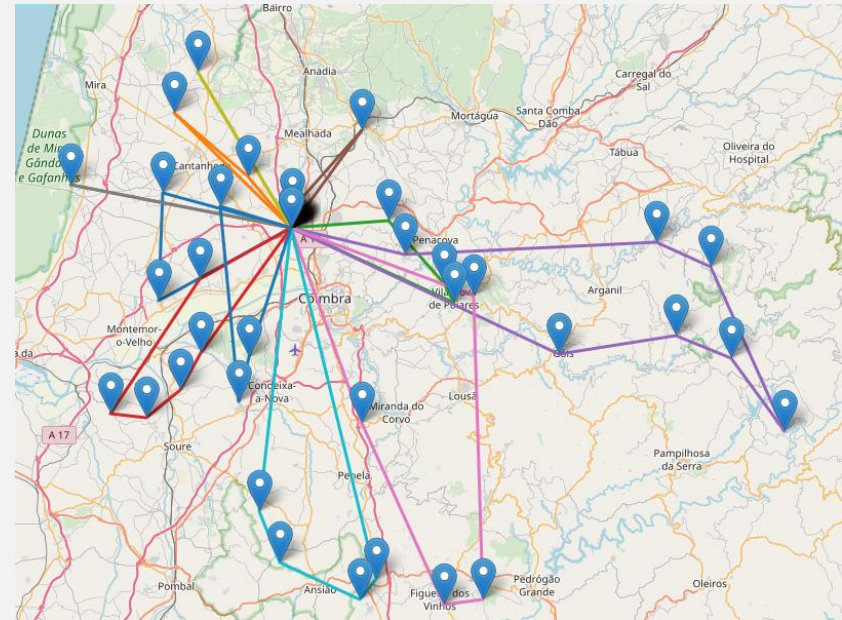
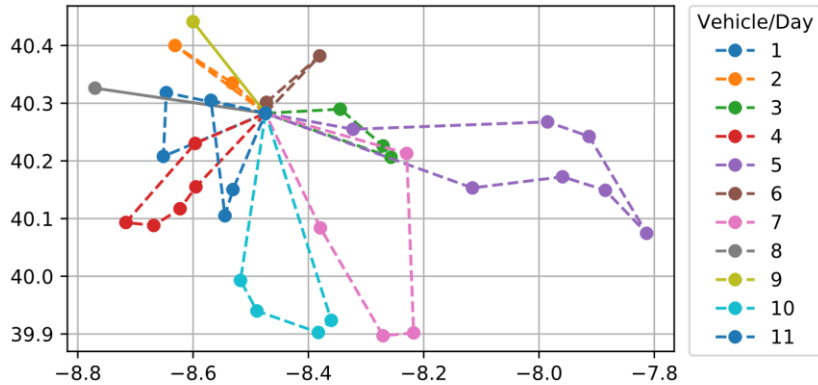
$$\text{A. Max } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right)$$

$$\text{B. Range } \sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right) - \min_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right)$$

# Baseline Results



## CVRP

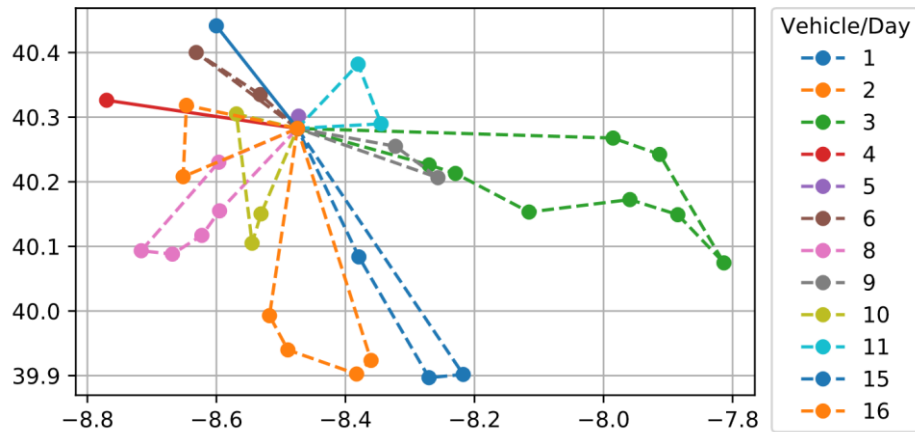


# Routes	Total Distance (km)	Total Duration (h)	Av. Route Demand (#Containers)	Av. Ruggedness
11	1 295,5	53,1	38	468

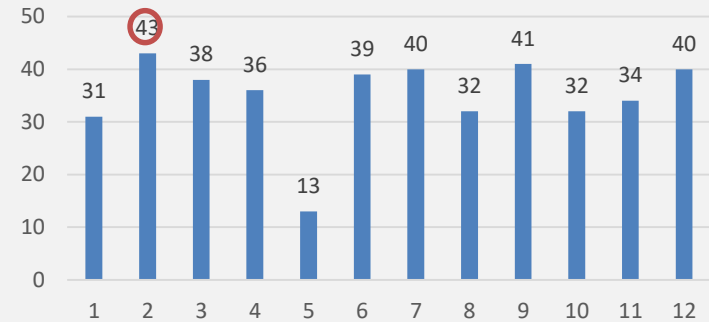
# Results I.A (Demand, min-max)



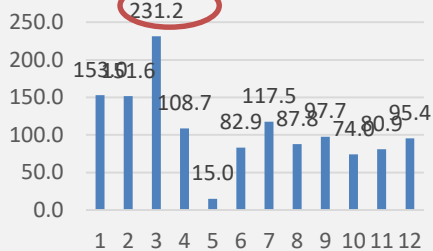
$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_i b_{ik} \times NbContainers_i \right)$$



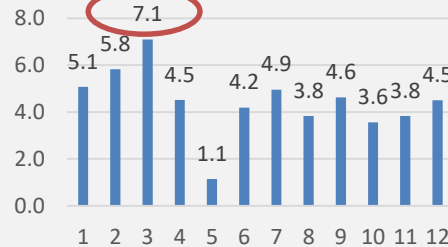
1.A Demand Workload



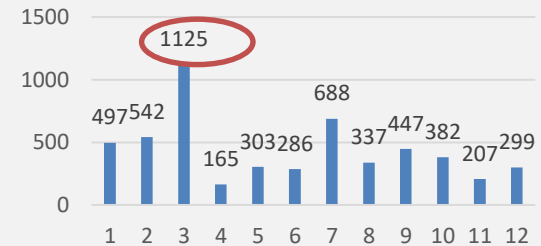
1.A Distance Workload



1.A Duration Workload



1.A Ruggedness Workload

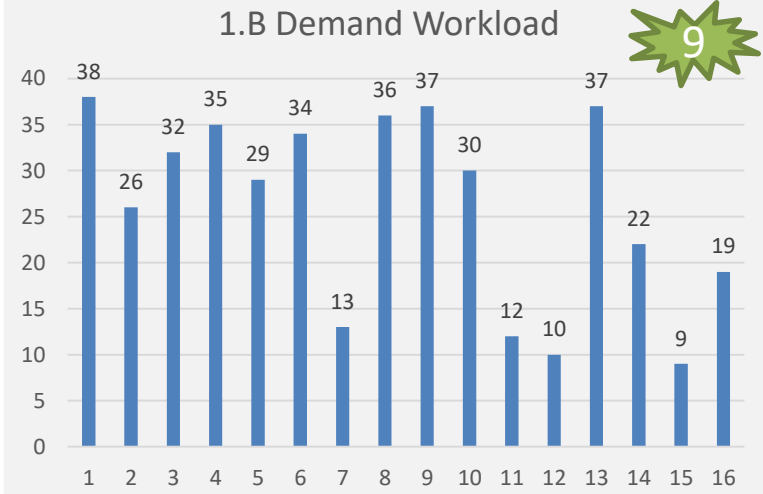
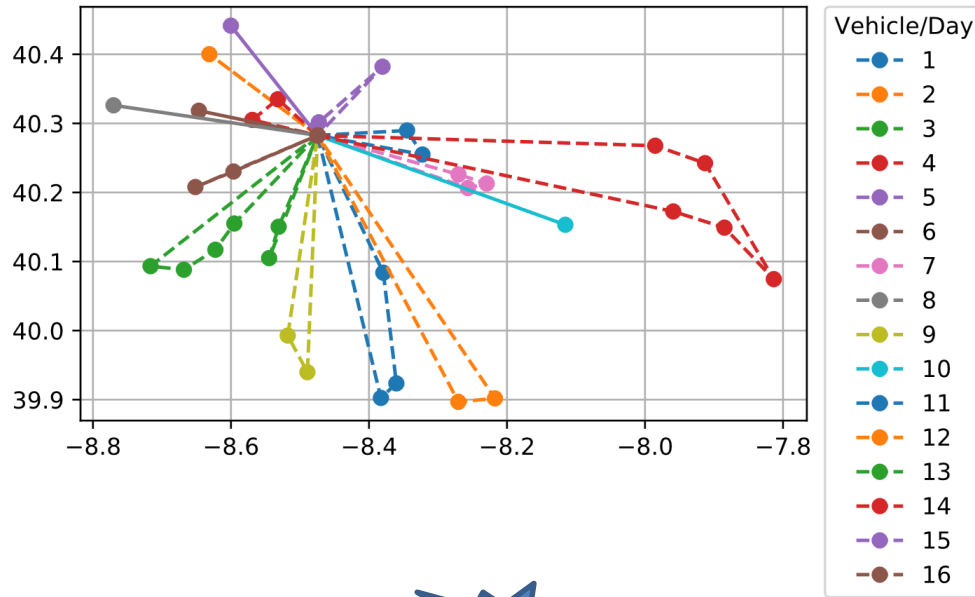




# Results I. B (Demand, Range)

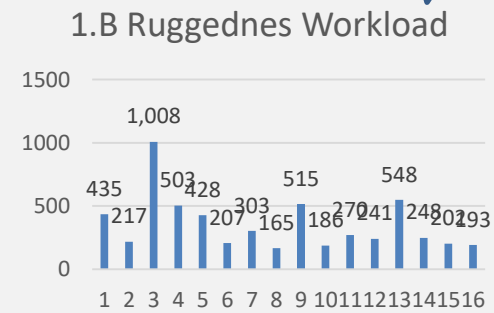
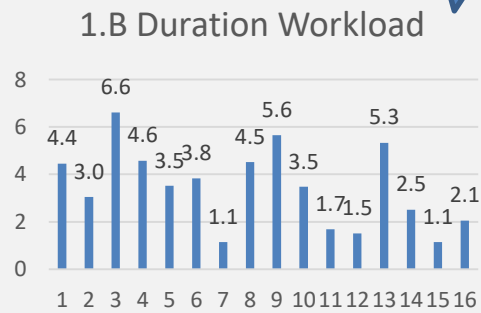
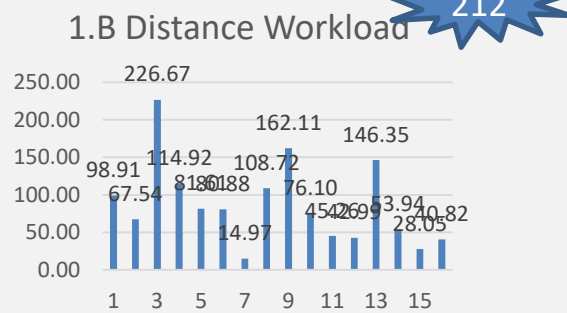


$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_i b_{ik} \times NbContainers_i \right) - \min_k \left( \sum_i b_{ik} \times NbContainers_i \right)$$



5,5

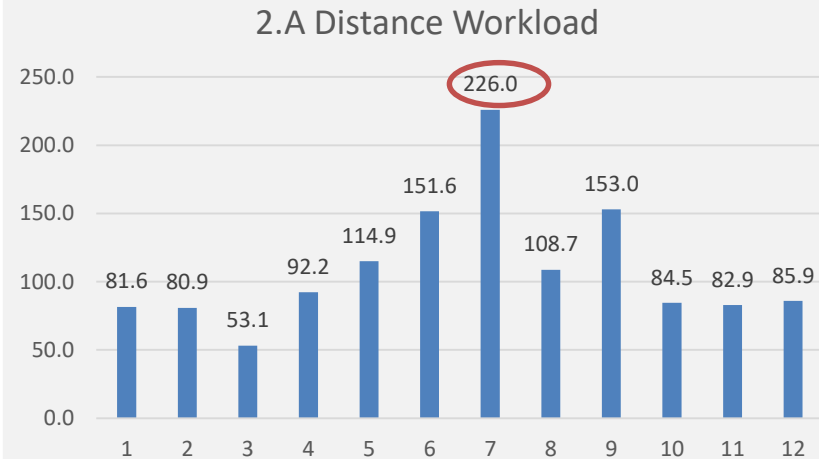
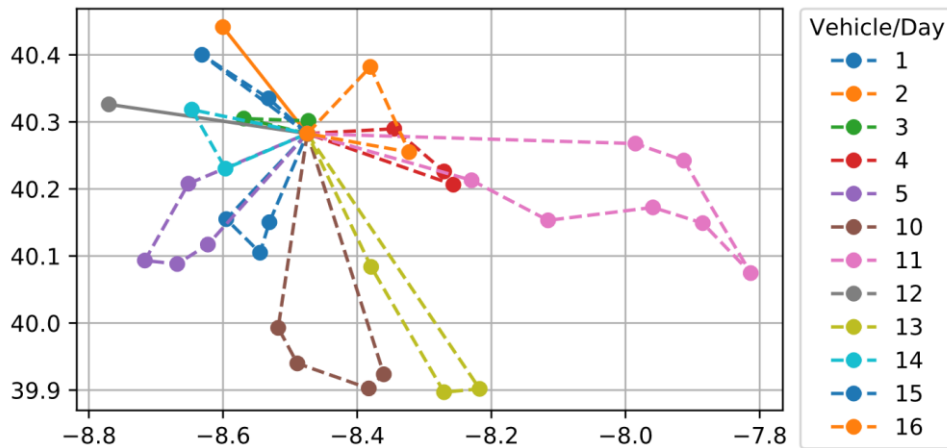
843



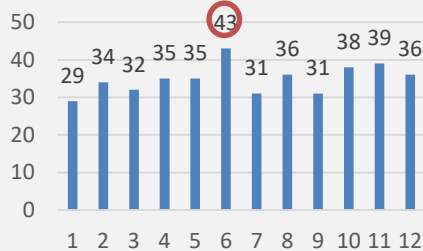
# Results 2.A (Distance, min-max)



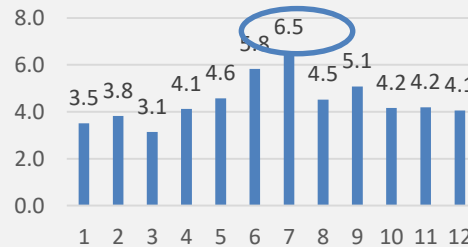
$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right)$$



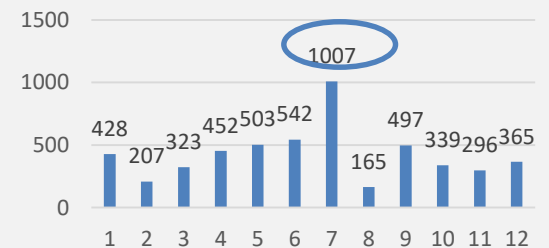
### 2.A Demand Workload



### 2.A Duration Workload



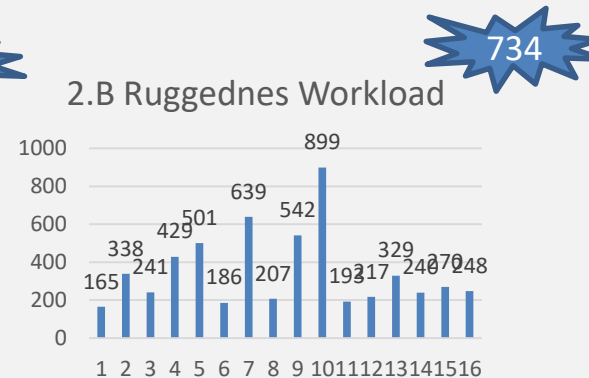
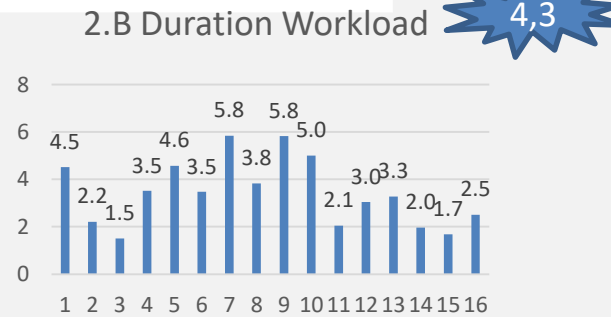
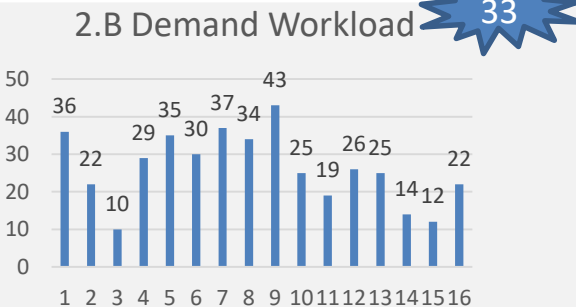
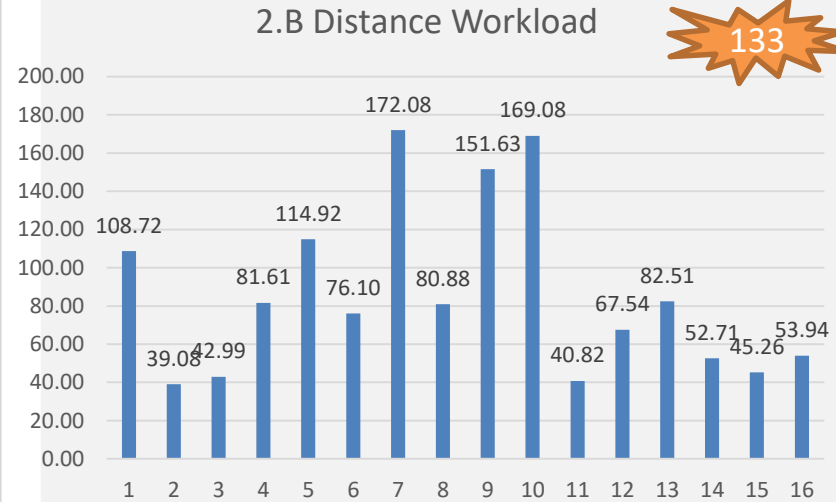
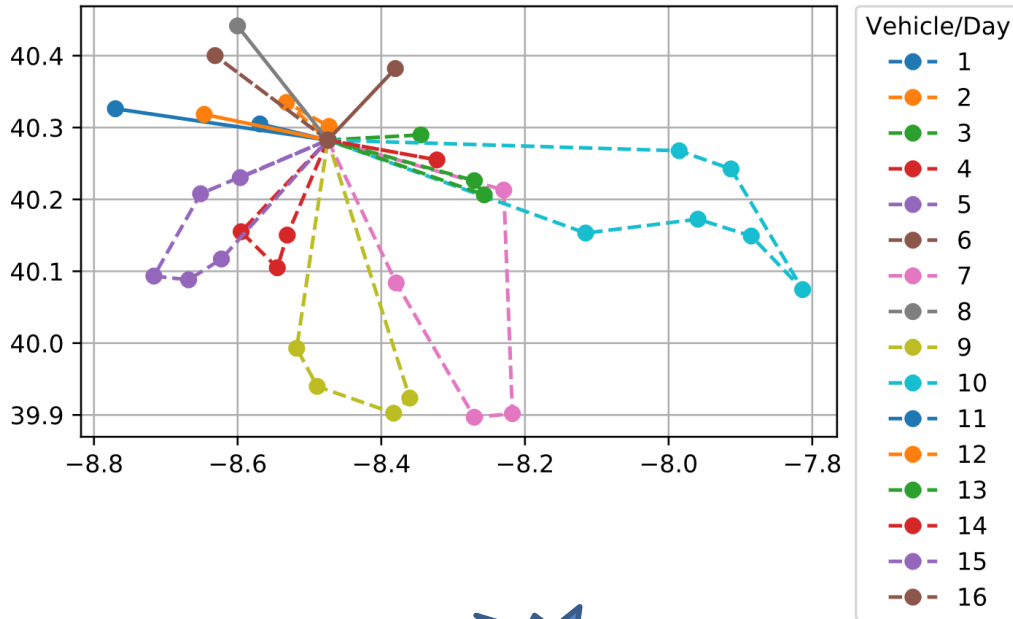
### 2.A Ruggedness Workload



# Results 2. B (Distance, Range)



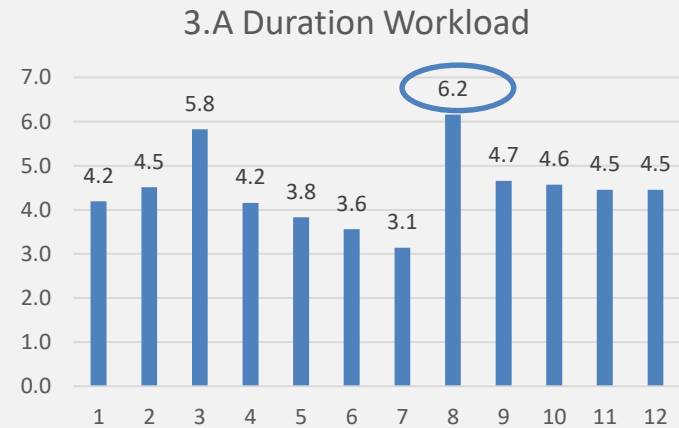
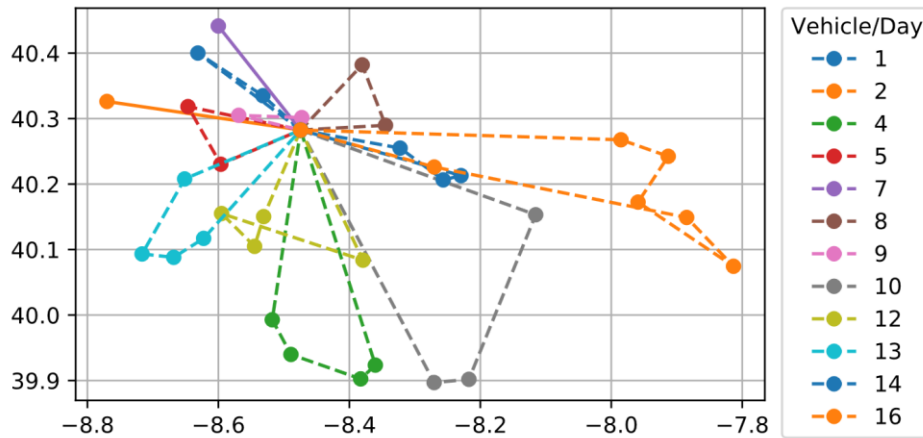
$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right) - \min_k \left( \sum_{ij} x_{ijk} \times d_{ij} + \sum_i b_{ik} \times NbContainers_i \times DBC \right)$$



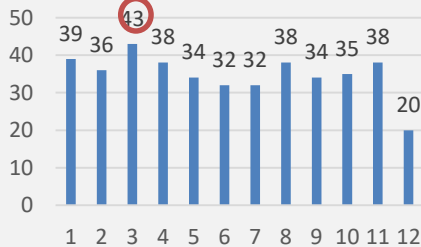
# Results 3.A (Duration, min-max)



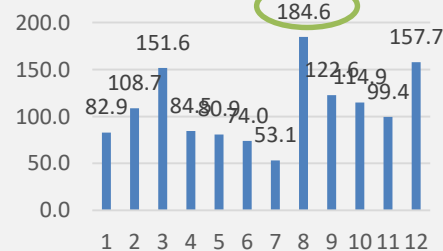
$Inter\ Distance\ TT + \max_k(Inter\ TT + IntraTT + Container\ Colection\ Time)$



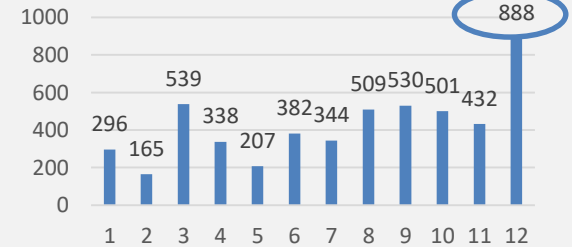
3.A Demand Workload



3.A Distance Workload



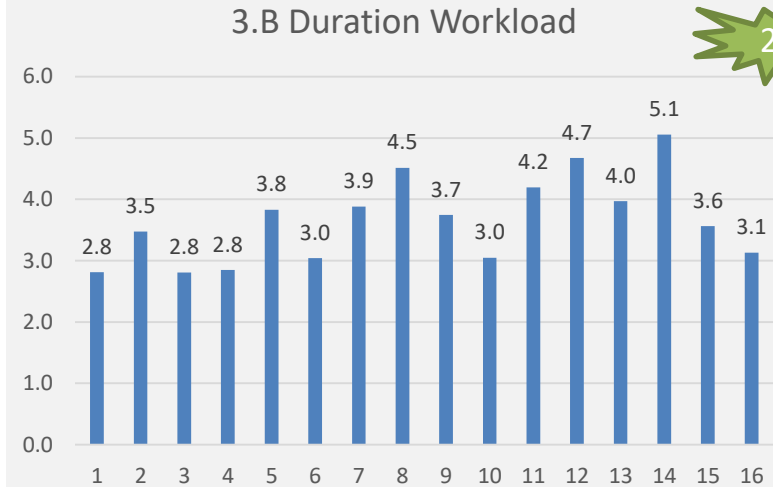
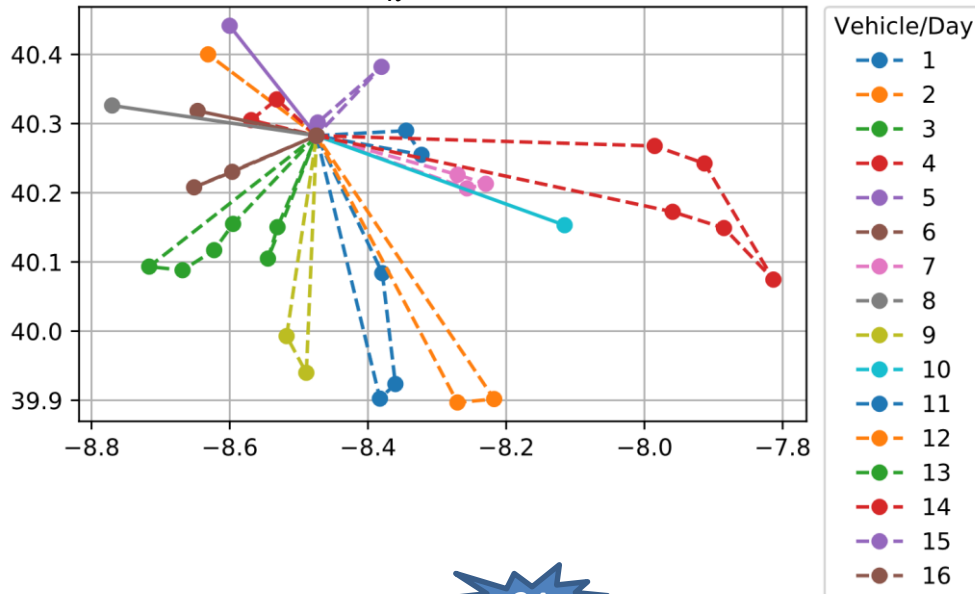
3.A Ruggedness Workload



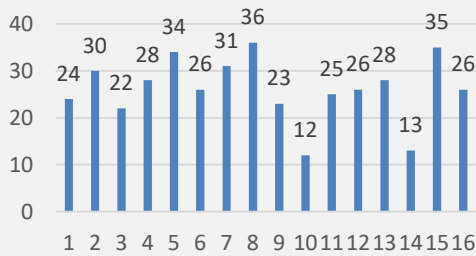
# Results 3. B (Duration, Range)



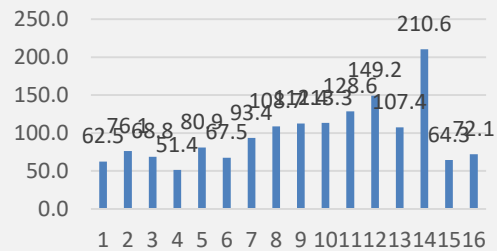
$$\text{Inter Distance TT} + \max_k(\text{Inter TT} + \text{IntraTT} + \text{Container Colection Time}) - \min_k(\text{Inter TT} + \text{IntraTT} + \text{Container Colection Time})$$



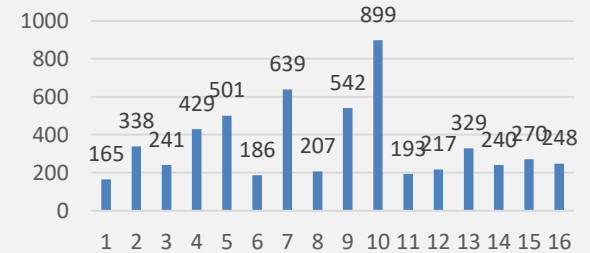
3.B Demand Workload



3.B Distance Workload



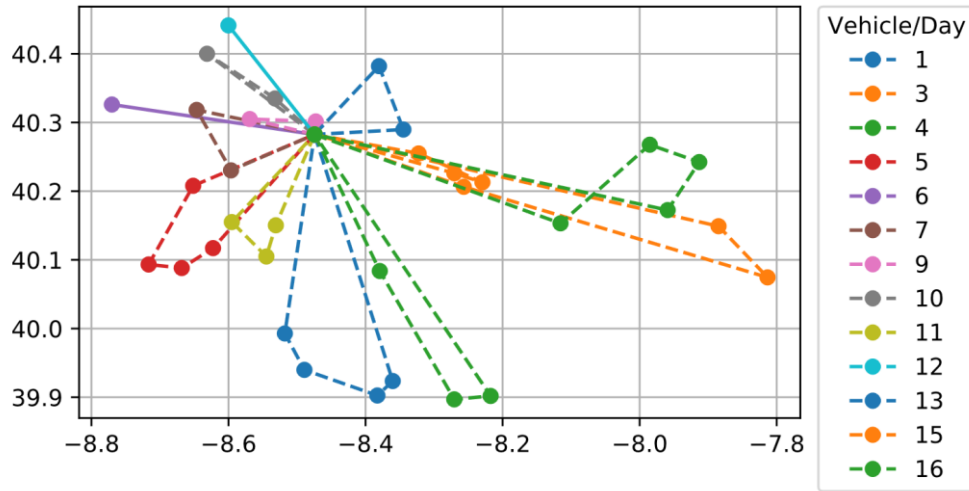
3.B Ruggednes Workload



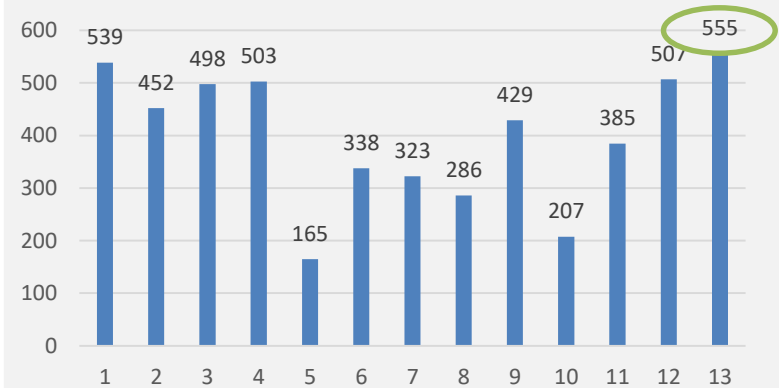
# Results 4.A (Ruggedness, min-max)



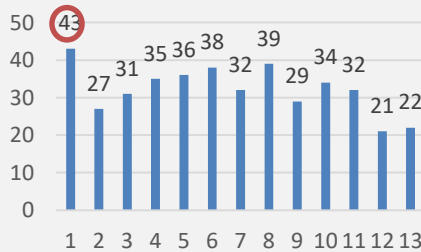
$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right)$$



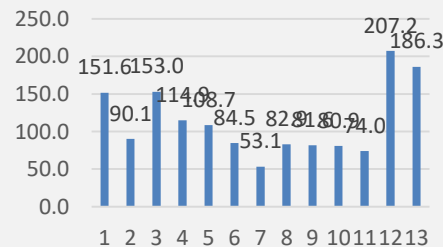
4.A Ruggedness Workload



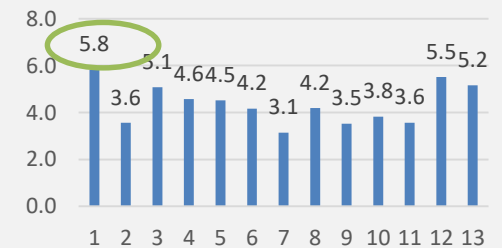
4.A Demand Workload



4.A Distance Workload



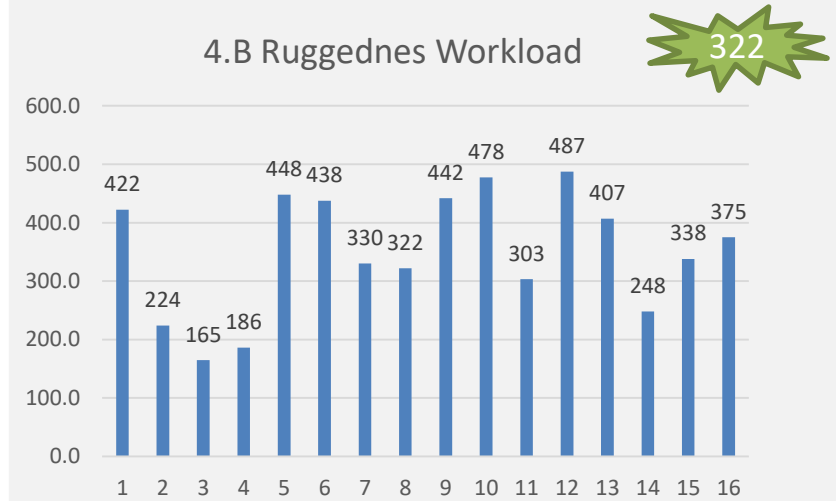
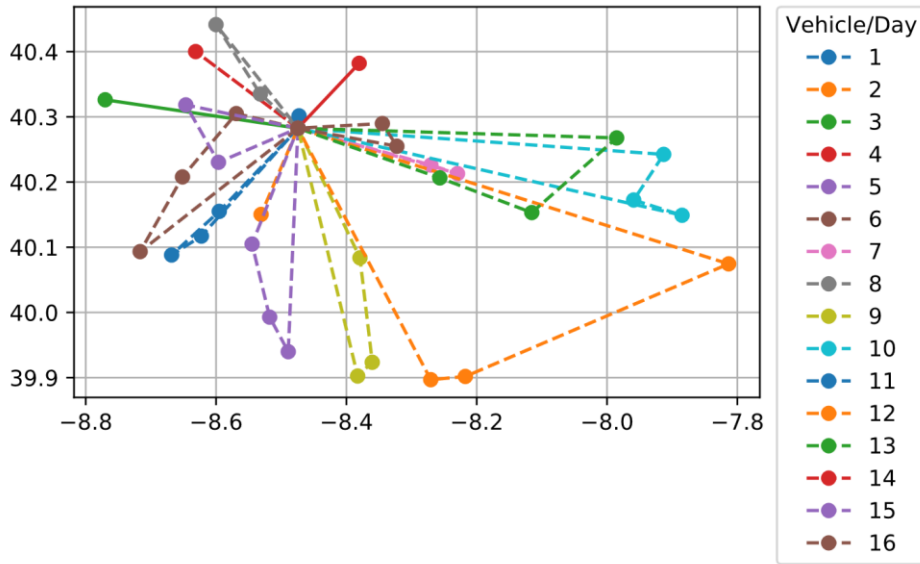
4.A Duration Workload



# Results 4. B (Ruggedness, Range)

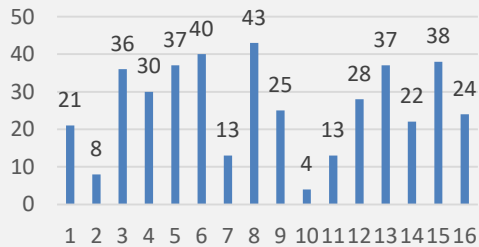


$$\sum_{ijk} x_{ijk} \times d_{ij} + \sum_{ik} b_{ik} \times NbContainers_i \times DBC + \max_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right) - \min_k \left( \sum_{ij} x_{ijk} \times coef_{ij} \right)$$



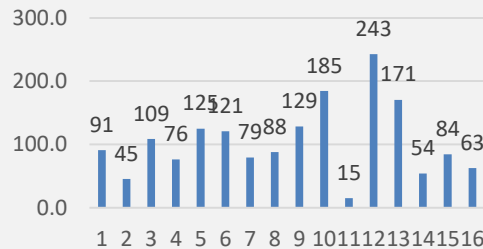
### 4.B Demand Workload

39



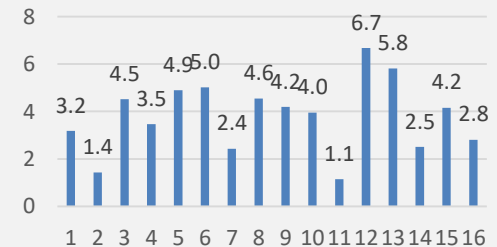
### 4.B Distance Workload

228



### 4.B Duration Workload

5.5



# Scenarios comparison to Baseline



	Total Distance (km)	Variation
Baseline	1 295,5	-
1.A	1 295,8	0%
1.B	1 389,8	7%
2.A	1 315,4	2%
2.B	1 379,9	6%
3.A	1 315,0	1%
3.B	1 567,2	17%
4.A	1 468,9	12%
4.B	1 676,2	23%



	#Routes	Variation
Baseline	11	-
1.A	12	8%
1.B	16	31%
2.A	12	8%
2.B	16	31%
3.A	12	8%
3.B	16	31%
4.A	13	15%
4.B	16	31%



**Total Distance:** Best results in terms of total distance associated to scenarios with function max and metric demand.

**Number of routes:** Range function always used the full set of routes (16). Scenario 4.A requires one more route to perform the collection.



# Scenarios comparison to Baseline



Total Duration (h) Variation		
Baseline	53,1	-
1.A	53,2	0%
1.B	55,0	3%
2.A	53,5	1%
2.B	54,8	3%
3.A	53,5	1%
3.B	58,6	9%
4.A	56,6	6%
4.B	60,8	13%



Ruggedness				
	Max	Variation	Range	Variation
Baseline	1037	-	872	-
1.A	1125	8%	960	-8%
1.B	1008	-3%	843	-23%
2.A	1007	-3%	842	-23%
2.B	899	-15%	734	-41%
3.A	888	-17%	723	-43%
3.B	759	-37%	594	-75%
4.A	555	-87%	390	-166%
4.B	487	-113%	322	-222%

**Total Duration:** Best total duration associated to scenarios with metrics demand and distance. However, the duration workload is more balanced.

**Ruggedness:** There is a compromise – Despite having the worst results in terms of cost, has a very high improvement in both workload functions.

# Conclusions



- In the literature, there are much more works with balancing concerns when heuristics are applied.
- The new metric, Ruggedness, associates, on average, higher coefficients to regions the partners empirically believe to have more ruggedness.
- Best results in terms of total distance/cost are associated to scenarios with function max and metric demand.
- Balancing newly introduced metric seems to have a great impact in the solution, implying a trade-off (scenarios that represent the greatest increase in cost but seem to have potential to improve social acceptance of routes)

# Future Work



- To solve the whole problem.
  - At this moment it is impossible to solve all of the scenarios for all of the clusters.
  
- Incorporate some of the workload into a VRPP model already published in the project.
  
- Add balancing functions associated with dispersion.
  - Absolute Deviation to the mean



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# *Waste Collection with Route Balancing Concerns: A real-world application*

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