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COIMBRA



## *Optimization-based Heuristics vs. Metaheuristics to solve the Smart Waste Collection Routing Problem*

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# WSmartRoute Project



Aims to explore a new paradigm that relies on **smart waste management**, where **real-time data** plays a central role in changing the way operations are managed today, **moving from static to dynamic routes**.

The tool to be developed will integrate **technology with management concerns** contributing to **improve the companies' operations decision-making process**.

<http://wsmartroute.tecnico.ulisboa.pt/>

# Agenda

Introduction

The Smart Waste Collection Routing Problem

Objectives

Optimization-based Heuristic Approach

Hybrid Simulated-Annealing/Local-Search Metaheuristic

Results for real-case instance

Conclusions

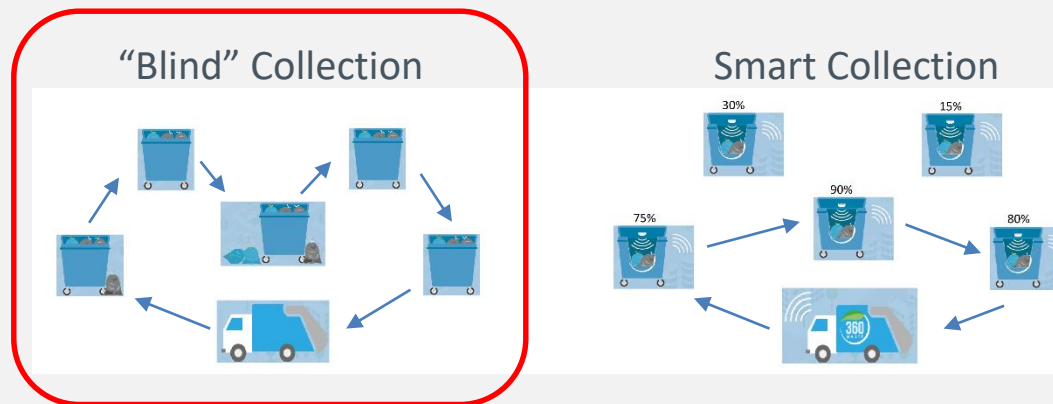
Future Work

# Introduction

Amount of **municipal solid waste** is highly variable and its accumulation is difficult to forecast<sup>1</sup>: **high uncertainty**.

**Waste management operations** are often related to **high inefficiency**: high transportation costs and high pollutant emissions.

“**Blind collection**”: static routes and vehicles visiting partially full bins.



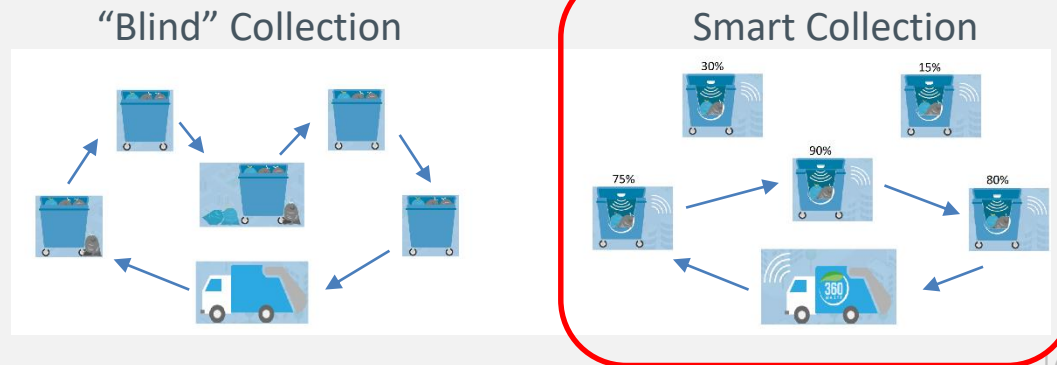
<sup>1</sup>(Nuortio et al., 2006)

# Introduction

Amount of **municipal solid waste** is highly variable and its accumulation is difficult to forecast<sup>1</sup>: **high uncertainty**.

**Waste management operations** are often related to **high inefficiency**: high transportation costs and high pollutant emissions.

**Smart Collection**: reduction of uncertainty and increase of collection operations' efficiency.



How?

<sup>1</sup>(Nuortio et al., 2006)

# The Smart Waste Collection Routing Problem

Use of **real-time information** on the bins' fill-level (transmitted by volumetric sensors placed inside the bins) to define **smart collection routes** that **maximize operational profit**<sup>2</sup>;

Max **PROFIT** = **revenues** obtained from the recyclable waste collected - **transportation costs** of collecting that waste

Maximize waste collected while minimizing distance travelled

Rather than simply selecting the fullest bins to be visited, and then apply VRP models to minimize the distance travelled

<sup>2</sup>(Ramos et al., 2018)

# The Smart Waste Collection Routing Problem

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Max **PROFIT** = **revenues** obtained from the recyclable waste collected - **transportation costs** of collecting that waste

**Decision:** To select the **waste bins to be visited** (if any) and the **optimal visiting sequence** in each day  $t$  for each vehicle  $k$ , which will **maximize the profit** while satisfying the vehicles' fixed capacity and the bins' capacity.

<sup>2</sup>(Ramos *et al.*, 2018)

# The Smart Waste Collection Routing Problem

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Defines when (in which day) the model should be run to maximize profit within a time horizon

**Solution Approach:**

Heuristic + VRP with Profit (VRPP) model<sup>2</sup>:

Model is solved at day  $t$ , in the morning, after receiving sensors' information on the bins' fill-level, when at least  $H$  waste bins are expected to overflow (to comply with the defined service level).

<sup>2</sup>(Ramos *et al.*, 2018)



# The Smart Waste Collection Routing Problem

Decision: To select the waste bins to be visited (if any) and the optimal visiting sequence in each day  $t$  for each vehicle  $k$ , which will maximize the profit while satisfying the vehicles' fixed capacity and the bins' capacity



## Solution Approach: Heuristic + VRP with Profit (VRPP) model<sup>2</sup>:

KPI	Day 1	Day 7	Day 12	Day 18	Day 24	Day 25	Day 30	Total	Average
Profit (€)	261.0	131.2	154.1	143.6	131.6	-59.9	111.3	872.9	124.7
Weight (kg)	5158.4	2644.0	4019.7	3625.6	2874.1	1310.6	2833.5	22465.8	3209.4
Distance (km)	229.0	120.0	227.8	200.9	141.5	184.4	157.9	1261.4	180.2
Attended bins	138	77	151	134	105	95	94	794	113
Ratio (kg/km)	22.5	22.0	17.6	18.1	20.3	7.1	17.9	17.8	17.8
<b>Gap</b>	<b>8.0%</b>	<b>11.0%</b>	<b>7.0%</b>	<b>15.3%</b>	<b>16.2%</b>	<b>58.6%</b>	<b>20.3%</b>	-	-
<b>Comp. Time (s)</b>	<b>14400</b>	<b>14400</b>	<b>14400</b>	<b>14400</b>	<b>14400</b>	<b>14400</b>	<b>14400</b>	<b>100800</b>	<b>14400</b>
Vehicles used	2	2	2	2	2	2	2	14	2

<sup>2</sup>(Ramos *et al.*, 2018)

**Problem: Low computational performance**

# Objectives

To propose two heuristic approaches to solve the SWCRP, improving the solution performance of the VRPP mathematical model.

- 1) Optimization-based heuristic
- 2) Hybrid simulated-annealing/local-search metaheuristic

## Optimization-based Heuristic



Decomposes the problem by **reducing the set of waste bins** to be inserted as input to the VRPP mathematical model

### Cluster First - Route Second:

selects a dynamic subset of waste bins to be considered, and then uses this dynamic set to feed the VRPP model that decides which waste bins are worth to be collected, considering their fill-levels and locations.

# Optimization-based Heuristic

VRPP model is combined with two heuristics:

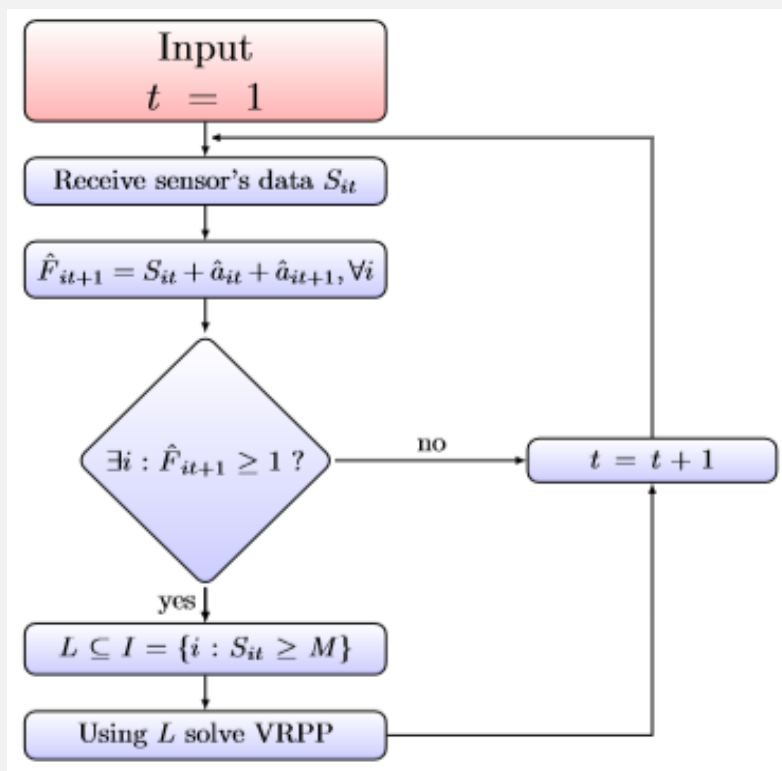
- 1) Waste bins are visited as late as possible

Heuristic procedure that defines when (in which day) the model should be run to maximize the profit within a time horizon;

- 2) Cluster First - Route Second

Heuristic rule that selects as a dynamic set of waste bins to be considered as an input for the VRPP model only those bins that have fill-levels higher than a defined threshold  $M$ .

Sensitive analysis



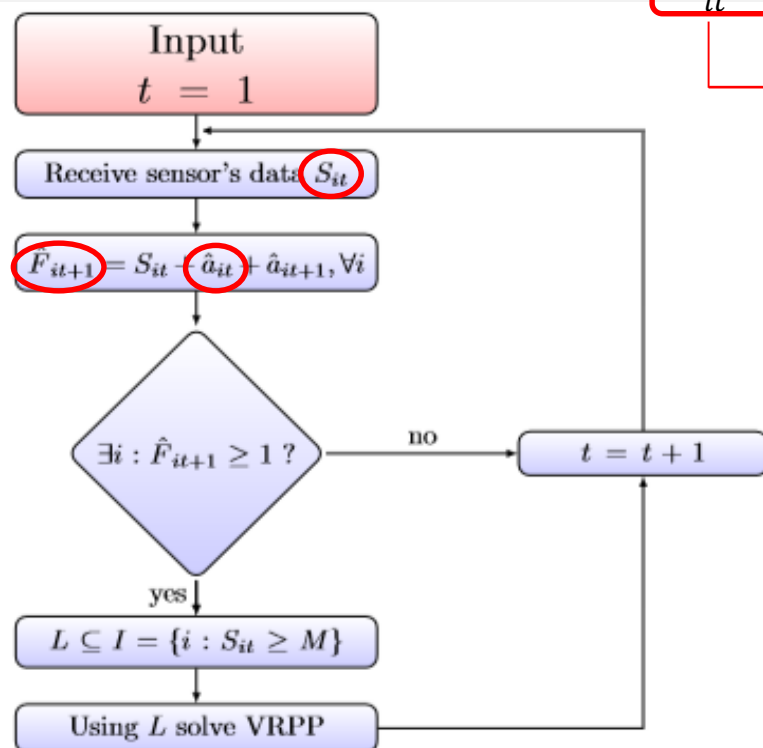
# Optimization-based Heuristic

$S_{it}$ : waste bins' fill-level → Sensors' information

$\hat{a}_{it}$ : expected daily accumulation rate

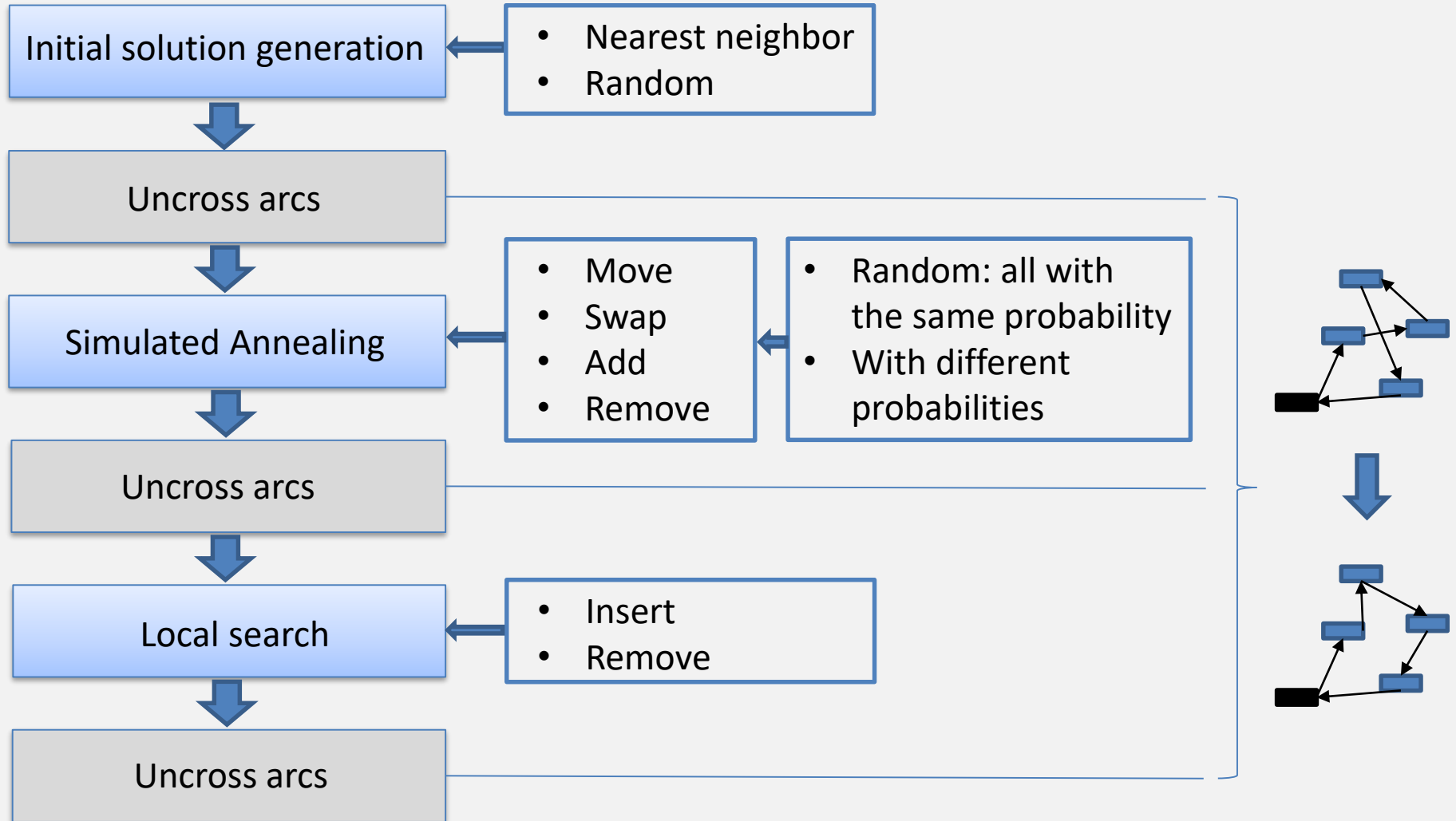
$\hat{F}_{it}$ : estimate of the waste bins' fill-level at the end of day  $t$

$\hat{F}_{it+1}$ : estimate of the waste bins' fill-level at the end of day  $t+1$



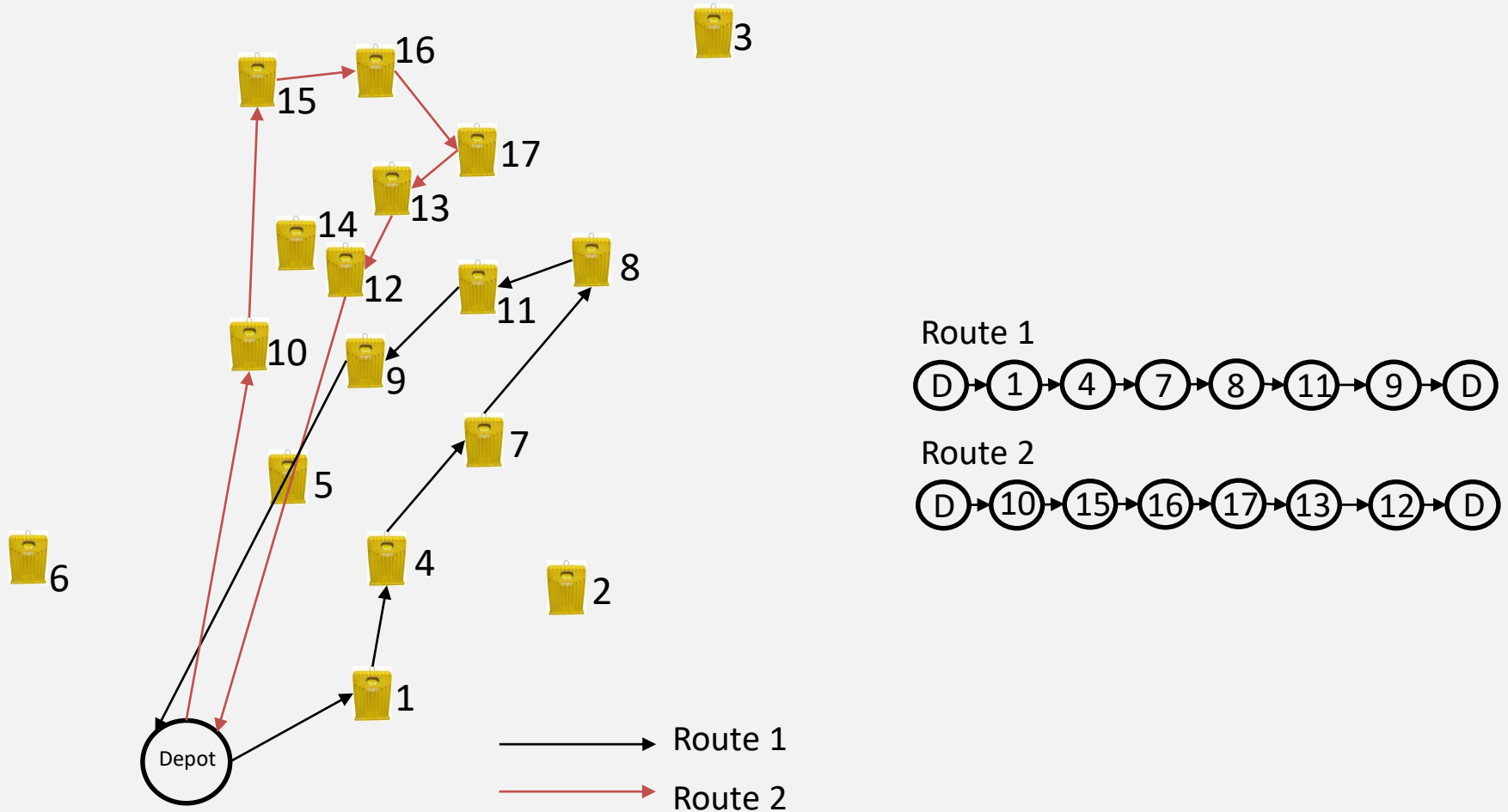
At day  $t$ , if there are waste bins about to overflow at  $t+1$ , then the waste bins for which the fill level  $S_{it}$  is higher than  $M$  are selected and, for those bins the model is solved and the routes are defined; if not, the next iteration is set to be carried out on the next day ( $t = t+1$ ).

# Hybrid Simulated-annealing / Local-search Metaheuristic



# Hybrid Simulated-annealing / Local-search Metaheuristic

Example

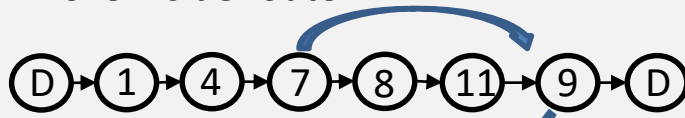


# Hybrid Simulated-annealing / Local-search Metaheuristic

## Simulated Annealing bin moving strategies

### Moving

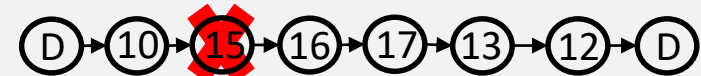
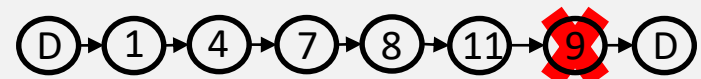
Move inside route



Move to another route

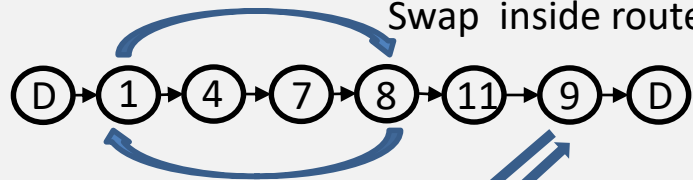


### Removing

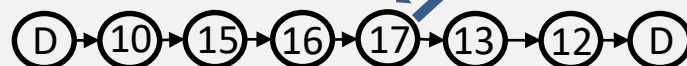


### Swapping

Swap inside route

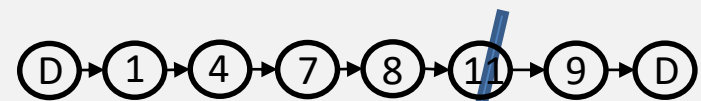


Swap from different routes

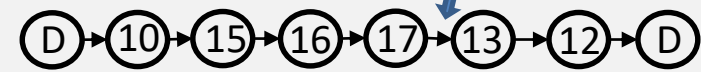


### Adding

Bins not in routes: 2, 3, 5, 6 and 14



Add bin 5 after bin 17





# Hybrid Simulated-annealing / Local-search Metaheuristic

## Local search bin moving strategies

### Inserting



50 closest bins: 50 closest bins:

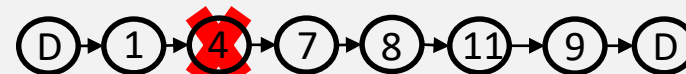
- |     |     |
|-----|-----|
| 1   | 11  |
| 6   | 17  |
| 4   | 7   |
| 5   | 13  |
| ... | ... |



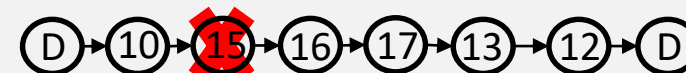
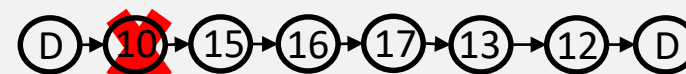
50 closest bins: 50 closest bins:

- |     |     |
|-----|-----|
| 1   | 17  |
| 6   | 14  |
| 4   | 12  |
| 5   | 16  |
| ... | ... |

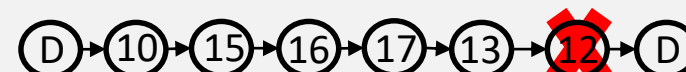
### Removing



...



...



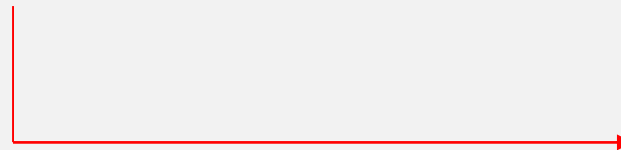
After each change OF is evaluated and new solution is only accepted if OF is improved

# Results for real-case instance

Case-study from a portuguese company responsible for the **recyclable waste collection** at 14 municipalities in Portugal;

Recyclable materials: **glass**, **paper/cardboard** and **plastic/metal**;

**Paper/cardboard**: 26 different static routes performed periodically.



Routes number 6, 11 and 13  
226 bins

3<sup>rd</sup> January 2013 - 2<sup>nd</sup> February 2013  
( $T = 30$  days)

Route 6 (68 bins): performed 2 times  
Route 11 (74 bins): performed 3 times  
Route 13 (84 bins): performed 5 times

# Results for real-case instance

Case-study from a portuguese company responsible for the **recyclable waste collection** at 14 municipalities in Portugal;

Recyclable materials: **glass, paper/cardboard** and **plastic/metal**;

**Paper/cardboard**: 26 different static routes performed periodically.

Date	03/01	09/01	10/01	10/01	17/01	21/01	24/01	24/01	01/02	01/02		
Route	Route 13	Route 11	Route 6	Route 13	Route 13	Route 11	Route 6	Route 13	Route 11	Route 13		
KPI	Day 1	Day 7	Day 8	Day 8.	Day 15	Day 19	Day 22	Day 22.	Day 30	Day 30.	Total	Average
<b>Profit (€)</b>	117.5	94.0	-73.2	112.1	125.5	74.9	-77.1	81.7	73.5	107.6	636.3	63.6
<b>Weight (kg)</b>	2471.8	2342.7	1420.4	2564.1	2693.2	2250.5	1512.6	2195.1	2213.6	2490.3	22154.3	2215.4
<b>Distance (km)</b>	117.3	128.6	208.2	131.5	130.4	138.9	220.8	126.9	136.8	129.0	1468.4	146.8
<b>Attended bins</b>	84	74	68	84	84	74	68	84	74	84	778	78
<b>Empty visited bins</b>	6	17	26	7	7	2	1	7	2	6	81	8
<b>Ratio (kg/km)</b>	21.1	18.2	6.8	19.5	20.7	16.2	6.9	17.3	16.2	19.3	15.1	15.1
<b>Vehicles used</b>	1	1	1	1	1	1	1	1	1	1	10	1
<b>Vehicles usage rate (%)</b>	61.8	58.6	35.5	64.1	67.3	56.3	37.8	54.9	55.3	62.3	-	55.4

66% of the collected waste bins had a fill-level equal or lower than 50%

# Results for real-case instance

## Optimization-based heuristic

$M=0%$  conceptually corresponds to the solution obtained in Ramos et al. (2018), where all bins are considered within the route definition - 226 bins

KPI	M = 0%							Total	Average	KPI	M = 10%						Total	Average
	Day 1	Day 6	Day 13	Day 20	Day 25	Day 30	Day 1				Day 6	Day 13	Day 19	Day 26	Day 29			
Profit (€)	253.1	186.9	224.4	223.9	147.9	106.7	1142.8	190.5	Profit (€)	253.9	187.4	219.2	181.6	195.4	38.8	1076.3	179.4	
Weight (kg)	3999.6	3990.5	3953.6	3998.6	3781.5	2865.3	22589.2	3764.9	Weight (kg)	3991.7	3968.0	3994.6	3994.6	3818.2	2490.9	22258.0	3709.7	
Distance (km)	126.8	192.2	151.2	155.9	211.3	165.5	1002.8	167.1	Distance (km)	125.3	189.5	160.3	197.8	167.2	197.8	1037.9	173.0	
Attended bins	98	118	121	119	136	97	689	115	Attended bins	88	112	119	140	111	113	683	114	
L	226	226	226	226	226	226	1356	226	L	124	121	154	165	158	131	853	142	
Ratio (kg/km)	31.5	20.8	26.2	25.6	17.9	17.3	22.5	22.5	Ratio (kg/km)	31.9	20.9	24.9	20.2	22.8	12.6	21.4	21.4	
Gap (%)	2.8	7.3	6.3	9.4	13.4	10.6	-	-	Gap (%)	0.0	2.6	5.8	7.8	5.9	27.9	-	-	
Computational time (s)	16201.2	16203.7	16200.4	16201.1	16204.4	16203.2	97213.9	16202.3	Computational time (s)	3275.0	16205.3	16201.2	16203.1	16202.2	16202.6	84289.3	14048.2	
Vehicles used	1	1	1	1	1	1	6	1	Vehicles used	1	1	1	1	1	1	6	1	
Vehicle Usage Rate (%)	99.99%	99.76%	98.84%	99.97%	94.54%	71.63%	-	94.12%	Vehicle usage rate (%)	99.79%	99.20%	99.86%	99.86%	95.46%	62.27%	-	92.74%	

KPI	M = 20%						Total	Average	KPI	M = 30%					Total	Average	
	Day 1	Day 6	Day 13	Day 20	Day 25	Day 29				Day 1	Day 7	Day 13	Day 19	Day 25			Day 29
Profit (€)	253.9	166.1	193.8	220.6	137.8	80.3	1052.5	175.4	Profit (€)	238.8	178.2	196.3	199.8	172.6	3.0	988.8	164.8
Weight (kg)	3991.7	3657.5	3616.4	3995.9	3409.1	2754.1	21424.8	3570.8	Weight (kg)	3976.8	3488.2	3421.9	3998.4	3512.2	1677.0	20074.5	3345.7
Distance (km)	125.3	181.3	149.7	159.0	186.0	181.2	982.5	163.8	Distance (km)	139.0	153.1	128.8	180.0	161.0	156.2	918.0	153.0
Attended bins	82	90	114	104	110	100	600	100	Attended bins	75	70	82	95	87	43	452	75
L	114	98	137	132	135	114	730	122	L	96	78	96	129	98	53	550	92
Ratio (kg/km)	31.9	20.2	24.2	25.1	18.3	15.2	21.8	21.8	Ratio (kg/km)	28.6	22.8	26.6	22.2	21.8	10.7	21.9	21.9
Gap (%)	0.0	3.6	4.8	4.6	5.4	13.3	-	-	Gap (%)	0.0	5.5	0.0	4.2	0.0	75.0	-	-
Computational time (s)	883.7	16208.9	16204.7	16203.0	16202.9	16200.1	81903.3	13650.5	Computational time (s)	6717.8	16210.0	1547.8	16203.9	1846.7	16200.0	58726.3	9787.7
Vehicles used	1	1	1	1	1	1	6	1	Vehicles used	1	1	1	1	1	1	6	1
Vehicle usage rate (%)	99.79%	91.44%	90.41%	99.90%	85.23%	68.85%	-	89.27%	Vehicle usage rate (%)	99.42%	87.20%	85.55%	99.96%	87.80%	41.93%	-	83.64%

KPI	M = 40%						Total	Average	KPI	M = 50%										Total	Average		
	Day 1	Day 7	Day 13	Day 25	Day 29	Day 1				Day 6	Day 8	Day 13	Day 15	Day 17	Day 19	Day 21	Day 22	Day 25	Day 30				
Profit (€)	230.5	142.8	213.2	196.5	167.2	10.1	960.3	160.0	Profit (€)	206.1	69.2	29.2	152.1	3.8	44.6	3.2	41.4	-48.5	34.9	197.0	732.9	66.6	
Weight (kg)	3858.9	3092.0	3534.0	3929.3	3315.9	1965.6	19695.7	3282.6	Weight (kg)	3882.3	1398.6	1504.3	3065.0	520.3	1959.0	559.2	1537.4	689.8	1822.8	3383.4	20321.9	1847.4	
Distance (km)	136.1	150.9	122.5	176.7	147.7	176.6	910.5	151.7	Distance (km)	162.7	63.7	113.7	139.0	45.6	141.5	49.9	104.6	114.0	138.2	124.3	1197.1	108.8	
Attended bins	71	62	70	83	69	45	400	67	Attended bins	68	24	29	55	10	38	32	10	14	36	60	376	34	
L	88	56	77	89	83	49	442	74	L	72	34	38	61	25	43	22	41	17	44	70	467	42	
Ratio (kg/km)	28.4	20.5	28.8	22.2	22.4	11.1	21.6	21.6	Ratio (kg/km)	23.9	22.0	13.2	22.1	11.4	13.8	11.2	14.7	6.0	13.2	27.2	17.0	17.0	
Gap (%)	0.0	6.4	0.0	2.1	1.4	0.0	-	-	Gap (%)	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	5.0	4.0	0.0	0.0	
Computational time (s)	4415.6	16213.2	3847.6	16212.2	16203.6	96.4	56988.6	9498.1	Computational time (s)	197.2	3.7	123.3	1275.6	3.5	28.8	0.7	45.3	2.3	16228.3	16200.0	34108.8	3100.8	
Vehicles used	1	1	1	1	1	1	6	1	Vehicles used	1	1	1	1	1	1	1	1	1	1	1	1	11	1
Vehicle usage rate (%)	96.47%	77.30%	88.35%	98.23%	82.90%	49.14%	-	82.07%	Vehicle usage rate (%)	97.06%	34.96%	37.61%	76.62%	13.01%	48.97%	13.98%	38.43%	17.24%	45.57%	84.58%	-	46.19%	

# Results for real-case instance

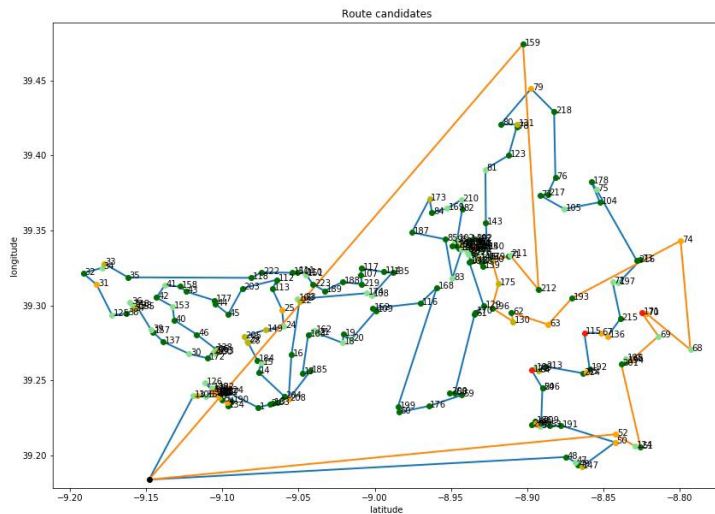
## Hybrid simulated-annealing/local-search metaheuristic

KPI	Day 1	Day 5	Day 6	Day 12	Day 15	Day 20	Day 24	Day 28	Day 30	Total	Average
Profit (€)	250.4	57.4	80.4	162.6	81.9	171.9	53.3	98.3	-22.8	933.4	103.7
Weight (kg)	3951.1	1112.0	2315.5	3063.4	2156.1	3901.4	1794.1	2819.6	218.0	21331.2	2370.1
Distance (km)	125.2	48.2	139.5	128.4	122.8	198.6	121.3	169.4	43.4	1097.7	121.9
Attended bins	105	30	83	93	92	126	79	102	9	719	80
Ratio (kg/km)	31.6	23.1	16.6	23.9	17.6	19.6	14.8	16.6	5.0	18.8	18.8
Comp. time (s)	2000	1400	1500	1700	1700	1900	1700	1800	1400	15000	1700
Vehicles used	1	1	1	1	1	1	1	1	1	9	1
Vehicles usage rate (%)	98.8	27.8	57.9	76.6	53.9	97.5	44.9	70.5	5.5	-	59.3

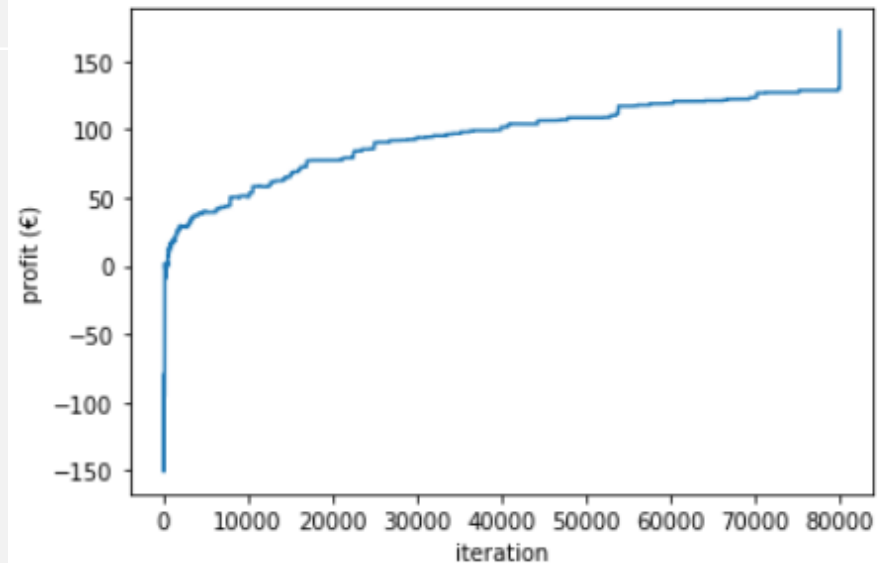
# Results for real-case instance

Hybrid simulated-annealing/local-search metaheuristic

KPI	Day 1	Day 5	Day 6	Day 12	Day 15	Day 20	Day 24	Day 28	Day 30	Total	Average
Profit (€)	250.4	57.4	80.4	162.6	81.9	171.9	53.3	98.3	-22.8	933.4	103.7
Weight (kg)	3951.1	1112.0	2315.5	3063.4	2156.1	3901.4	1794.1	2819.6	218.0	21331.2	2370.1
Distance (km)	125.2	48.2	139.5	128.4	122.8	198.6	121.3	169.4	43.4	1097.7	121.9
Attended bins	105	30	83	93	92	126	79	102	9	719	80
Ratio (kg/km)	31.6	23.1	16.6	23.9	17.6	19.6	14.8	16.6	5.0	18.8	18.8
Comp. time (s)	2000	1400	1500	1700	1700	1900	1700	1800	1400	15000	1700



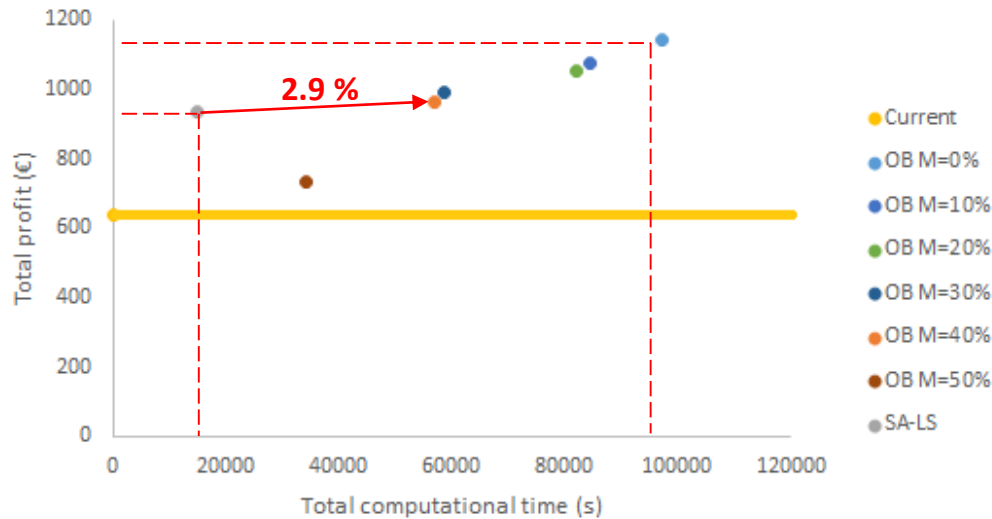
Profit evolution for the best solutions in successive iterations



# Results for real-case instance

## Comparison: Profit versus Computational time

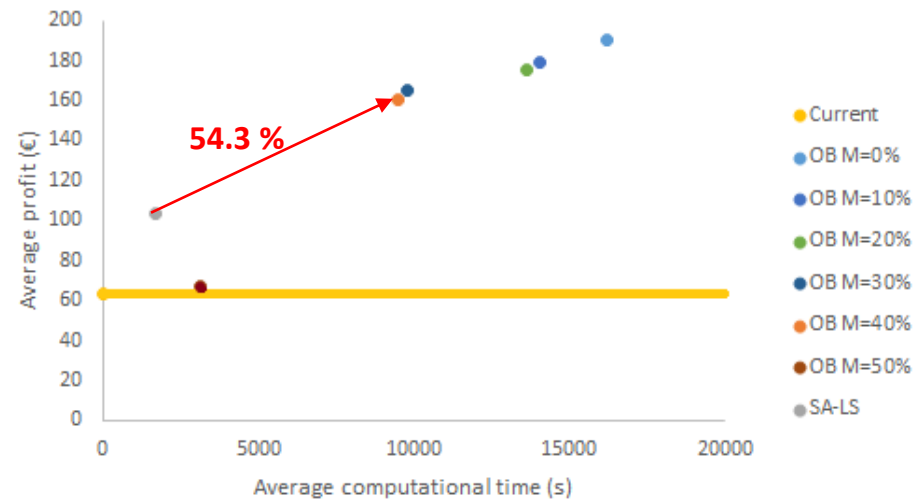
### Total



KPI	Current situation - Total	OB - M=0% - Total	OB - M=40% - Total	SA-LS - Total
Profit (€)	636.3	1142.8	960.3 <b>2.9 %</b>	933.4
Attended bins	778	689	400	719
Number of routes	10	6	6	9
Ratio (kg/km)	15.1	22.5	21.6	18.8
Comp. time (s)	-	97213.3	56988.6 <b>3.8 x</b>	15000
Vehicles used	10	6	6	9
Vehicles usage rate (%)	-	-	-	-

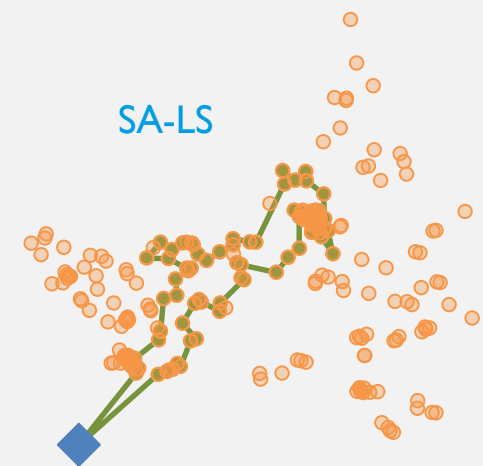
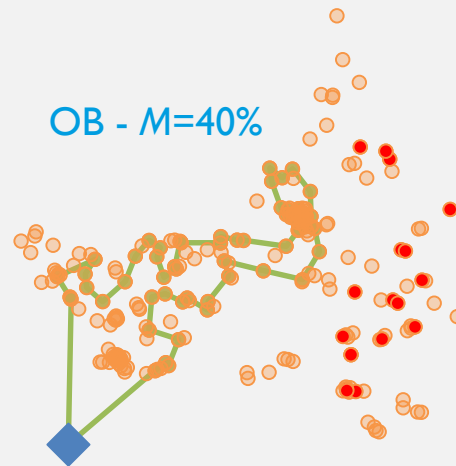
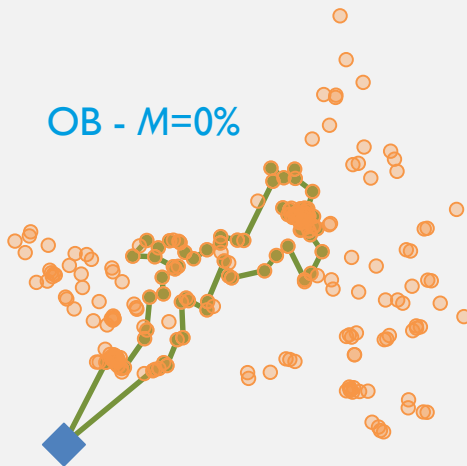
### Average



KPI	Current situation - Average	OB - M=0% - Average	OB - M=40% - Average	SA-LS - Average
Profit (€)	63.6	190.5	160.0 <b>54.3 %</b>	103.7
Attended bins	78	115	67	80
Number of routes	1	1	1	1
Ratio (kg/km)	15.1	22.5	21.6	18.8
Comp. time (s)	-	16202.3	9498.1 <b>5.6 x</b>	1700
Vehicles used	1	1	1	1
Vehicles usage rate (%)	55.4	94.1	82.1	59.3



# Results for real-case instance

## Comparison: Day 1



KPI	OB - M=0%	OB - M=40%	SA-LS
Profit (€)	253.1 	230.5	250.4
Weight (kg)	3999.6	3858.9	3951.1
Distance (km)	126.8	136.1	125.2
Attended bins	98	71	105
L	226	88	226
Ratio (kg/km)	31.5	28.4	31.6
Gap (%)	2.8	0	-
Comp. time (s)	16201.2	4415.6	2000 
Vehicles used	1	1	1
Vehicles usage rate (%)	99.9	96.5	98.8



# Conclusions

To solve the SWCRP, two new solution approaches were proposed: an optimization-based heuristic and a hybrid simulated-annealing/local-search metaheuristic;

- both approaches define more profitable routing plans comparing with the current situation: improvements from 47% to 80%;
- considering the optimization-based heuristic, the sensitive analysis on the threshold  $M$  shows that: as  $M$  increases, less computational time is required, but lower profits are obtained;
- the hybrid simulated-annealing/local-search metaheuristic proved to be faster than the optimization-based heuristic: 5 times faster;
- the optimization-based heuristic proved to find more profitable routes for the 30-day planning period than the hybrid simulated-annealing/local-search metaheuristic: 54% more profitable.

- Improving the **optimization-based heuristic** to consider not **only the fill-levels**, but also the **locations**;
- improving the **hybrid simulated-annealing/local-search metaheuristic** by **changing parameters**;
- exploring the **balance between routes**, limiting shift time;
- exploring **Inventory Routing Problem** models that allow a **weekly profit maximization** instead of daily.

# THANK YOU FOR YOUR ATTENTION!



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